CHARACTERIZATION OF INTERPOLATION BETWEEN GRAND, SMALL OR CLASSICAL LEBESGUE SPACES

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Abstract In this talk we show that the interpolation spaces between Grand, small or classical Lebesgue are the so called Lorentz-Zygmund spaces or more generally $G\Gamma$ -spaces. As a direct consequence of our results, any Lorentz-Zygmund space $L^{a,r}(LogL)^{\beta}$ is an interpolation space in the sense of Peetre either between two Grand Lebesgue spaces or between two small spaces, provided that $1 < a < \infty, \beta \neq 0$. The method consists in computing the so called K-functional of the interpolation space and in identifying the associated norm.