## Delsarte's extremal problem and packing on locally compact Abelian groups

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Let G be a locally compact Abelian group, and let  $\Omega_+$ ,  $\Omega_-$  be two open sets in G. We investigate the constant  $\mathcal{C}(\Omega_+, \Omega_-) = \sup \{ \int_G f : f \in \mathcal{F}(\Omega_+, \Omega_-) \}$ , where  $\mathcal{F}(\Omega_+, \Omega_-)$ is the class of positive definite functions f on G such that f(0) = 1, the positive part  $f_+$  of f is supported in  $\Omega_+$ , and its negative part  $f_-$  is supported in  $\Omega_-$ . In the case when  $\Omega_+ = \Omega_- =: \Omega$ , the problem is exactly the so-called Turán problem for the set  $\Omega$ . When  $\Omega_- = G$ , i.e., there is a restriction only on the set of positivity of f, we obtain the Delsarte problem. The Delsarte problem in  $\mathbb{R}^d$  is the sharpest Fourier analytic tool to study packing density by translates of a given "master copy" set, which was studied first in connection with packing densities of Euclidean balls.

We give an upper estimate of the constant  $C(\Omega_+, \Omega_-)$  in the situation when the set  $\Omega_+$  satisfies a certain packing type condition. This estimate is given in terms of the asymptotic uniform upper density of sets in locally compact Abelian groups.

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