# Mathematical Ideals in Coimbra

## September 2012

#### **Tuesday, September 25: 16.30-18**

A short history of ring ideals, modules, normal subgroups, boolean filters et similia in classical modern algebra, (they are all "the same thing" in a way...), and of their calculus: product, residuals, etc.

#### Wednesday, September 26: 14-17

Short, crash course in Universal Algebra (notations and key notions: 1/2 hour). Generalization of normal subalgebras and ideals in universal algebras: (Higgins) in Omega-groups, (Magari) in functionally complete universal algebras, (Ursini) in general pointed varieties. The (pointed) categorical generalizations of normal subobject, of ideals, and of clots. Bonus: HANPs= hints at the non-pointed case.

### Thursday, September 27: 9-12

A useful property for ideals to be normal in the pointed case: subtractive varieties, and their properties, and subtractive categories. The commutator of ideals, in varieties. A Conceptual Ladder of notions (pointed case) for varieties and –in some instances— for categories:

- subtractive (S) (Theorem: <==> 0-permutable congruences);
- 0-regular (0-R);
- ideal determined (ID) ( Theorem:  $\langle ==> 0-R+S \rangle$ ;
- 0-coherent (0-Coh)(Theorem : <==> ID + Mal'cev )
- classically ideal determined (CID)(Theorem: <==> semiabelian )
- abelian

Bonus: HANPs.

## Friday, september 28: 14-16

Several articulations of "coherence". Characterizing varieties of Abelian (Omega-) groups in ideal theoretic terms.